

Η Χρέωση ως Μηχανισμός Ελέγχου Δικτύων

*Κωνσταντίνος Κουρκουμπέτης, Βασίλειος Σύρης
και Γεώργιος Δ. Σταμούλης*

Why Charge for Telecommunication Services ?

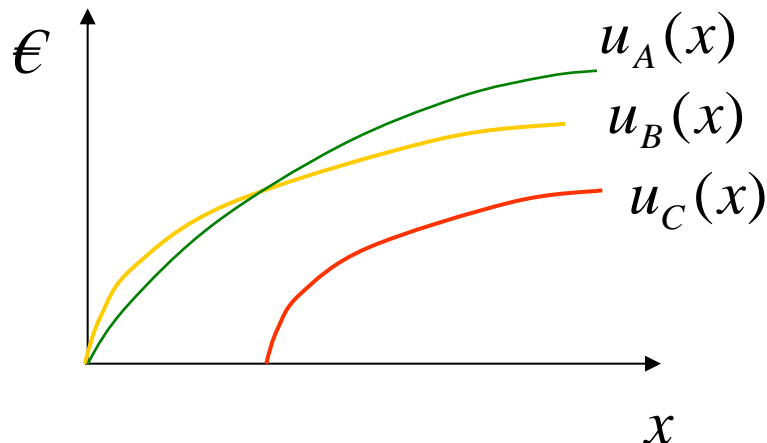
- In order for the Network (or Service) Provider to:
 - Recover costs
 - Make profits and save capital for future expansion
 - Control the system:
 - examples: charging of applications for admission to U.S. university
 - charging for street-parking in a city
 - Obtain **information** from users
 - examples: special call packages for long-distance fixed telephony or for mobile telephony
 - their adoption is indicative of user's type and *future* behavior

Terminology

- **price**: correlated with service unit
 - E.g. €/Mbyte or €/callminute
- **tariff**: charge structure
 - more general form of charging (i.e., $a+px$)
 - control mechanism
- **charge**: total amount that must be paid

Utility function

- Each consumer is characterized by a utility function $u(x)$
 - Translates into monetary units the benefit/satisfaction of the consumer from the use of the particular network resource or service
 - Expresses consumer's willingness-to-pay
 - Can also have the meaning of benefit from trading, reselling



$$u_A(10) = 5, u_B(10) = 2$$

Charging Components

1. Fixed charge

→ e.g.: monthly flat rate charging of Internet access

2. Usage charge

→ e.g.: fixed telephony is charged on time and distance

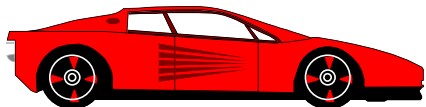
- may be hard to quantify the “unit” of usage
- E.g. bursty traffic should not be charged on volume only, because it is harder to multiplex than a constant-rate traffic stream (generating the same volume), and thus “consumes” more resources.

Charging Components

3. Congestion charge
→ its level depends on the congestion encountered or caused, similarly to highway tolls
 4. Quality charge → often combined with usage or flat charges
- A charge of a telecommunication service constitutes a **combination** of the above components
- Examples: a) monthly flat charge of Internet access depends on access rate, i.e. on a “quality” factor.
- b) Often, the following combination applies:
- Usage + Congestion + Quality → Variable charge

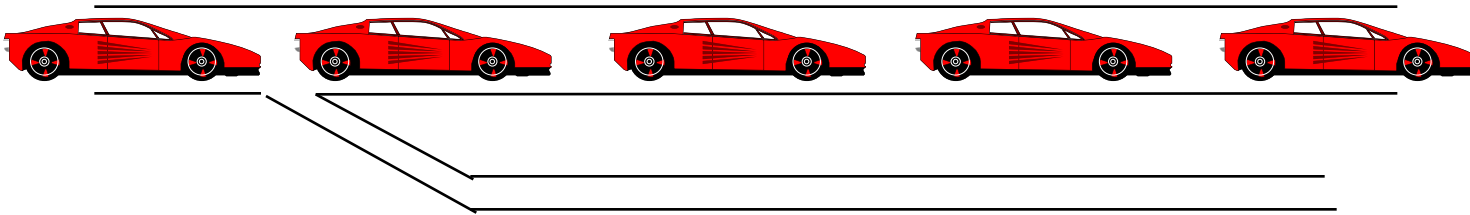
Congestion Charge

- Depends on **congestion** *during* service
- Applies to cases where:
 - everyone can be served, but
 - congestion results in service quality **degradation**
E.g. highways, Internet
- Example: Charging access to highways, according to the a priori set congestion charge

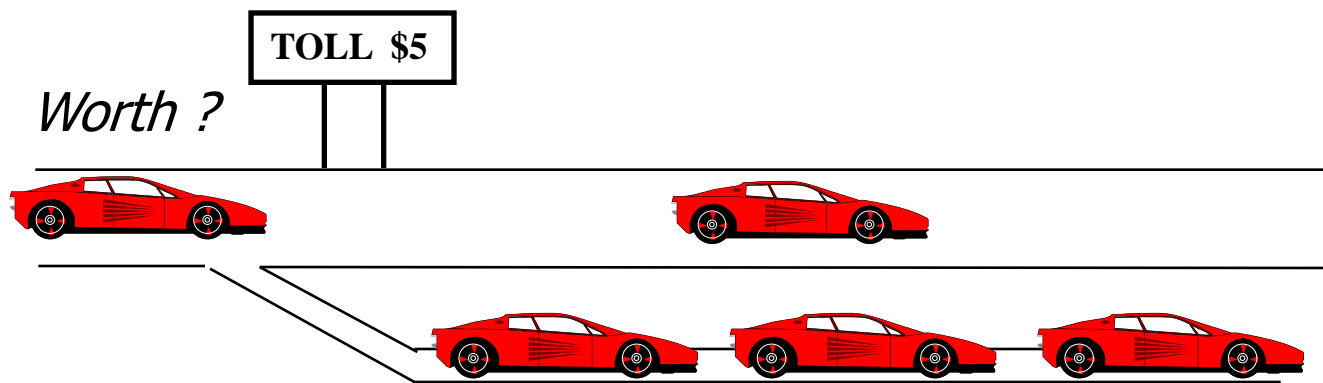


Congestion Charge (continued)

- Free access → traffic in highway is heavy

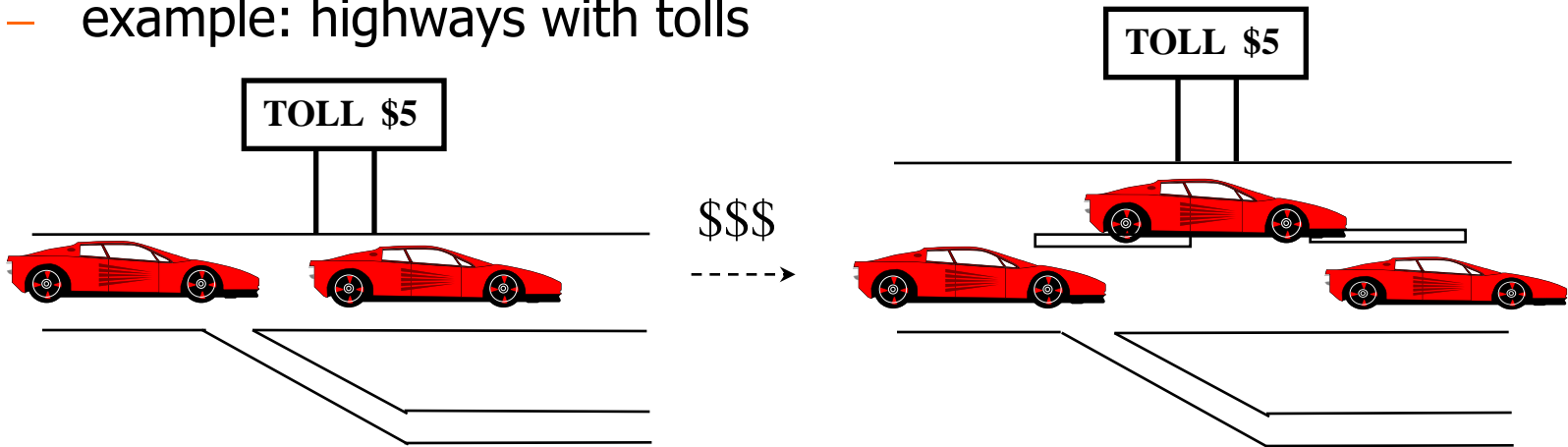


- Paid Access → traffic in highway is lighter



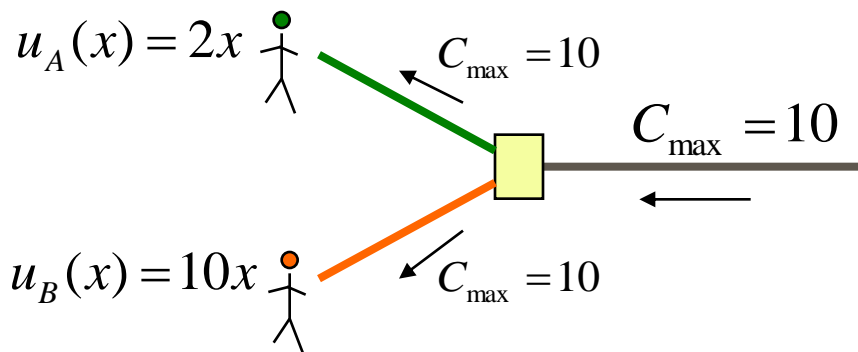
Capacity Expansion

- A network provider should expand capacity upon **congestion**
 - **social welfare** can be further increased, *despite* the cost for additional capacity
- Economic theory suggests that expansion can be funded by re-investing the revenue from **congestion charges**
 - example: highways with tolls



Fixed and Variable charges

- Fixed charge: related to connection cost
- Variable charge: related with the size of consumption
 - Recovery of usage cost,
 - **Control** mechanism (of priority) of consumer



Cost = 1€ /unit

Connection Cost = 5€

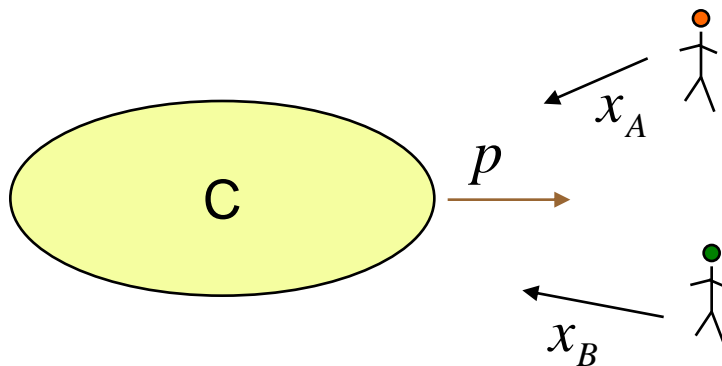
Cost based charging: $5 + x$

Every user receives $x = C_{\max} / 2 = 5$

Is it economically optimal ?

Pricing as a control mechanism (I)

- Service provider does not know the utility function of the consumers
- Consumers are pursuing their own benefit
- The quantity of the available service is finite
- How can the total benefit of the consumers be maximized? The network profit?
- **Pricing Mechanism!**

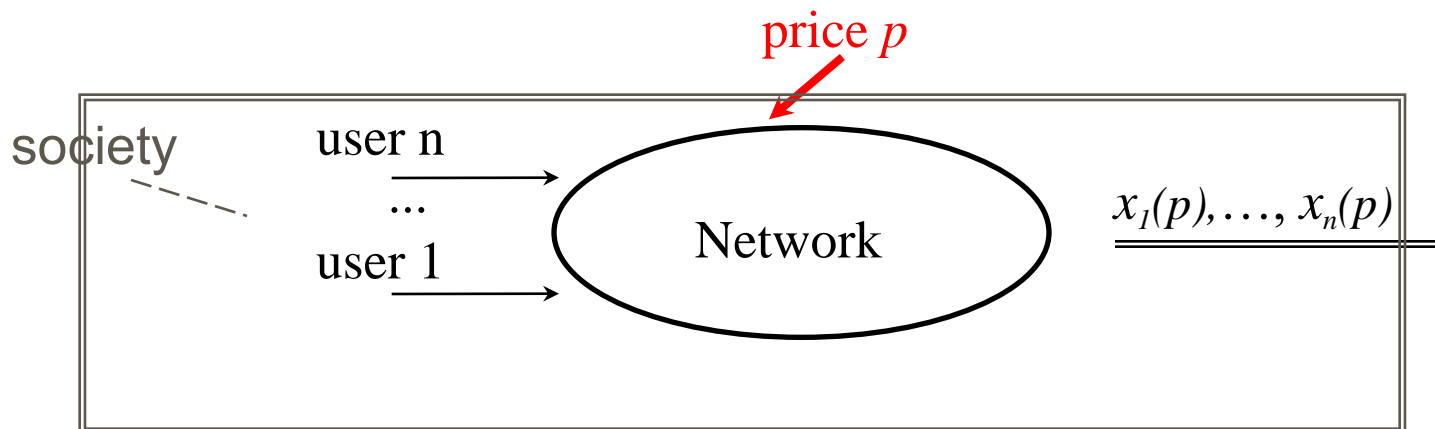


How much should I ask if the price is p ?

How is the problem specialized for networks ?

Charging as Control Mechanism

- Charges can be used as an internal control mechanism of the system **provider & users** to reach the **social optimum**
- Example: Socially Optimal Bandwidth Allocation
 - Network Provider sells bandwidth at a **price p** per kbps,
 - **Given** this price, each user i selects amount $x_i(p)$ of kbps purchased
 - Provider pays for capacity with the revenue collected
 - There exists an **equilibrium price p** that leads to **social optimum**, i.e. maximizes the sum of user utilities (= **social welfare**)



More formally (I)

- One link, with capacity C shared by users with concave utility functions
- **Social welfare** maximization problem:

$$\max_{\{x_i\}} \sum_i u_i(x_i) \quad s.t. \quad \sum_i x_i \leq C \quad (1)$$

- Mathematical solution (requires global information)
→ Maximize the Lagrangian

$$\max_{\{\lambda, x_i\}} L(\lambda, \{x_i\}) = \sum_i u_i(x_i) - \lambda(\sum_i x_i - C)$$

The optimal point of (1) is characterized by $\lambda, \{x_i\}$ for which:

$$\sum_i x_i = C, \quad \frac{\partial u_i}{\partial x_i} = \lambda$$

More formally (II)

- **Distributed** solution of the problem with **economic** mechanism \rightarrow use price $p = \lambda$
- The user solves his **own net benefit maximization**:
 $\max[u_i(x_i) - px_i]$ the condition for which is: $\frac{\partial u_i}{\partial x_i} = p$
- Price p **discovered** iteratively by means of **tatonnement** process \rightarrow provider updates market price p in order to “lead” total demand to become equal to the capacity C .
- Under general market conditions the market price p converges to the price λ of the centralized problem (i.e. the Lagrange multiplier)
 - Approach extended by Kelly et al. to **networks**

Incentives

- A charging scheme influences users' **demand**, according to the incentives it offers to the user for **individual** optimization
- Each individual user's behavior influences the **social well-being (welfare)**
- A charging scheme is incentive compatible if **individual** user optimization also results in **social** optimization
 - Applies to mechanism of slide 14

Examples of Incentives

- **Wrong** Incentives
 - Monthly flat charge for Internet access
 - DSL connections left permanently open, thus giving rise to the need for more ports in the DSLAMs
 - Free night use of mobile telephones (U.K. – late 1990s)
 - *blocking*: telephones were left open for long hours

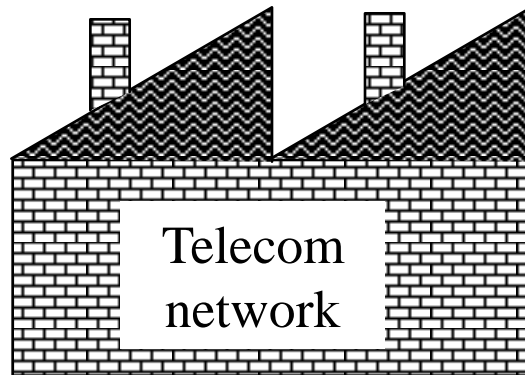
Examples of Incentives

- **Right Incentives**

- Combination of Usage- and congestion-based charging of Internet
 - considered as an effective way to avoid congestion
- Time-of-day charging in telephony and power
 - shifting of non-business calls off the peak period
 - satisfaction of both business and non-business users

Story on Charging Internet and Broadband Services

- “produces” services
from **shared** resources
- **usage** is hard to quantify
 - **cost** is hard to share



network theorists

- write articles

network engineers

- technical standards
- may leave concrete charging solutions for later

economists

- complex economic models
- overlook many critical details of technology