MutaLog: a Tool for Mutating Logic Formulas

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Abstract—Assessing the quality of a test suite is an important step of the testing process. Indeed, it is necessary to ensure that the different test cases target all the critical parts of the system. Model-based testing is a famous technique to perform testing. It uses a model of the system under test. Most of these models include logic formulas. Such formulas encompasses constraints to be satisfied within a system, e.g., an expected behavior or particular conditions to be fulfilled at a given stage of the execution. One way to evaluate the quality of a test suite with respect to these logic constraints is to use mutation analysis. This technique has been proven to be effective for evaluating the quality of a test suite in both model-based and non-model-based testing. However, while many mutation analysis tools exist, none of them performs on logic formulas. Towards this direction, this paper introduces MutaLog, an open source tool which allows performing mutation analysis on logic formulas.

I. INTRODUCTION

Testing a system is important to ensure both its correctness and reliability [1]. In order to provide a high confidence in the testing process, it is important to make certain that the quality of the test suite is high. Getting the expected output with a test suite targeting only the trivial part of the system is pointless. As a result, it is necessary to guarantee that the different test cases are targeting all the critical parts of the system.

Model-based testing is a famous technique to perform testing [2]. To this end, it uses a model of the system under test from which test cases are derived. Most of the software models include logic formulas. Such formulas encompasses constraints to be satisfied within a system, e.g., an expected behavior or particular conditions to be fulfilled at a given stage of the execution. For instance, the activation of a particular module in the system requires another module to be enabled.

One way to evaluate whether such model constraints are satisfied during the testing process is to use mutation analysis [3], [4], [5]. Mutation analysis aims at evaluating the quality of test suites. It is generally applied on programs and it involves the modification of the original software artifact into altered versions. Each of this altered version is called a mutant. Each mutant encompasses a defect willingly introduced. The test suite is then evaluated on these mutants to establish whether or not they are able to reveal the introduced defects. With this respect, the artifact on which we apply mutation analysis is a logic formula. Thus, a mutant is an altered version of this formula.

Mutagenesis has been applied to various models, e.g. Feature Models [6], Finite State Machines [7], Petri nets [8] or security policies metamodels [9]. While tools exist to perform mutation analysis on programs and software models, there is no tool available to the authors knowledge to perform mutation analysis of logic formulas. Here, it should be noted that the scope of the tool is bounded to formulas derived from models. This means that the formulas represent constraints that must always hold. In this respect, the present paper introduces MutaLog, an open source tool which allows performing mutation analysis on logic formulas.

The remainder of this paper is organized as follows. Section [II] shows the adoption of MutaLog. Section [III] presents the concepts underlying the approach performed by the tool and Section [IV] describes the approach itself. Section [V] introduces the functionalities, architecture and usage of the tool. Finally, Section [VI] discusses related work before Section [VII] concludes the paper.

II. ADOPTION OF MUTALOG

MutaLog has been adopted in several work. In [10], it is used to transform the logic formula representing a model for software product line in order to produce a more accurate model of the system. The transformation are made on the logic constraints of the model. Another application of the tool aims at creating mutants of a logic formula to assess the quality of software product line test suites [6]. The results of this work show that the mutants employed by the tool are effective to characterize a test suite. In particular, the diversity of the test suite is linked with its ability to detect mutants.

Recently, it has been shown that measuring the number of model-based defects gives a stronger correlation to code-level faults than measuring the number of the exercised t-wise interactions in the context of Combinatorial Interaction Testing [11]. The defects introduced in the models are alterations of logic constraints, such as the mutation operators implemented by the tool.
III. BACKGROUND

A. Logic Formulas

In this paper, we use boolean logic formulas expressed in Conjunctive Normal Form (CNF). Such formulas are a conjunction of \( n \) clauses \( C_1, \ldots, C_n \), where a clause is a disjunction of \( m \) literals. A literal is a variable or its negation. Thus, a CNF formula \( \phi \) is of the form:

\[
\phi = \bigwedge_{i=1}^{n} \left( \bigvee_{j=1}^{m} l_j \right), \quad \text{where } l_j \text{ is a literal.}
\]

For instance, the following boolean CNF formula \( \psi = (a \lor b) \land c \land (b \lor \neg c) \) has 3 variables: \( a, b \) and \( c \), and 3 clauses: \( (a \lor b), c \) and \( (b \lor \neg c) \).

B. Test Case and Test suite

A test case is an assignment of the variables of a given formula. For instance, \( tc_1 = \{a = \text{false}, b = \text{true}, c = \text{true}\} \) is a test case for the above-mentioned formula \( \psi \).

We say that a test case satisfies a formula if the formula is evaluated to \( \text{true} \) with respect to the assignment of the test case. For instance, evaluating the formula \( \psi \) with the assignment of \( tc_1 \) leads to \( \psi = (\text{false} \lor \text{true}) \land \text{true} \land (\text{true} \lor \text{false}) = \text{true} \). As a result, \( tc_1 \) satisfies \( \psi \). On the contrary, \( tc_2 = \{a = \text{true}, b = \text{true}, c = \text{false}\} \) does not satisfy the formula \( \psi \) since it is evaluated to \( \psi = (\text{true} \lor \text{true}) \land \text{false} \land (\text{true} \lor \text{true}) = \text{false} \).

Similarly, we say that a test suite satisfies a formula \( \psi \) if any test case of the test suite satisfies \( \psi \). A test suite does not satisfy a formula \( \psi \) if at least one test case of this test suite does not satisfy \( \psi \). Since the formulas used by the tool are derived from models, the formula under test must be evaluated to \( \text{true} \).

C. Invalid Formula

We say a formula is invalid if there is no test case that can satisfy it. For instance, the formula \( \psi = a \land \neg a \) is invalid, i.e. can never be \( \text{true} \). In this work, since logic formulas are derived from models, invalid ones are meaningless.

D. Mutation Analysis

Mutation analysis forms a powerful technique with various applications like software testing \([12, 13]\) and debugging \([14]\). It is applied by creating altered (mutant) versions of the various programs artifacts like source code, specification models, etc. \([12, 13]\). The main idea behind this approach is to evaluate the power of test cases to reveal behavior differences between the original (unaltered) and the mutated (altered) artifact versions.

The mutated versions represent possible defects of the artifact under test and they are produced based on a set of well defined rules called mutant operators \([13]\). Mutant operators are defined on “syntactic descriptions to make syntactic changes to the syntax or objects developed from the syntax” \([13]\). The process of introducing mutants is called mutation analysis. The ability of the utilized test cases to reveal the introduced mutants is examined in order to use this approach for testing purposes (mutation testing). If a mutant can be detected by a test case, the mutant is called killed. Otherwise, it is called live. Therefore, measuring the ratio of the killed mutants to the totally introduced ones results in a quality measure of the testing process. This measure is called mutation score and demonstrates the ability of the tests to detect errors:

\[
\text{Mutation score} = \frac{\text{mutants killed}}{\text{total mutants} - \text{invalid mutants}}.
\]

It should be noted that invalid formulas are not taken into account since formulas are derived from models. In the context of this paper, mutants are produced by applying a set of mutant operators to the logic formula. The test case evaluation is performed by checking whether the test cases satisfy the formula, i.e. whether the formula is evaluated to \( \text{true} \). Consequently, a mutant is said to be killed if its formula is not satisfied, i.e. if the formula is evaluated to \( \text{false} \).

IV. APPROACH

The mutation analysis approach for logic formulas performed by the tool operates as follows. First, mutants of the considered logic formulas are created by applying different operators. Then, it is evaluated which mutants are killed by the test cases of the test suite. Finally, the mutation score is returned.

In this section, we will consider the following logic formula:

\[
\psi = (a \lor b) \land (\neg a \lor c)
\]

and the following test suite:

\[
T = \{tc_1, tc_2\}, \quad \text{where}
\]

\[
tc_1 = \{a = \text{true}, b = \text{true}, c = \text{true}\} \quad \text{and} \quad tc_2 = \{a = \text{true}, b = \text{false}, c = \text{true}\}
\]
as a running example.

A. Creation of Mutants of the Logic Formula

The first step of the approach creates mutants of the logic formula by applying different mutation operators on it. The

<table>
<thead>
<tr>
<th>Table I</th>
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<tbody>
<tr>
<td><strong>MUTANT OPERATORS FOR CNF LOGIC FORMULAS</strong></td>
</tr>
<tr>
<td><strong>Mutation Operator</strong></td>
</tr>
<tr>
<td>Literal Omission (LO)</td>
</tr>
<tr>
<td>Literal Negation (LN)</td>
</tr>
<tr>
<td>Clause Omission (CO)</td>
</tr>
<tr>
<td>Clause Negation (CN)</td>
</tr>
<tr>
<td>AND Reference (AR)</td>
</tr>
<tr>
<td>OR Reference (OR)</td>
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</tbody>
</table>
A. Features

The previous section. Mutation analysis approach for logic formulas presented in 2,000 lines of code christopherhenard/mutalog assignments of tc case exist, the mutant is said to be killed. test case that does not satisfy the formula. When such a test result, for each mutant, it is evaluated whether there is one to evaluate constrained boolean expressions, e.g. [17]. As a assignment of the test case. SAT solver are widely used evaluate the satisfiability of the formula given the variables mutant created there is one test case in the test suite that kills it. To this end, a satisfiability (SAT) solver is used to application of the operators can add or remove clauses within the formula. The last two operators transforms operators respectively remove and negate one literal or one clause. The application of these operators to the example formula = (¬a ∨ c), = (¬a ∨ b) ∧ ¬a ∨ c ... 6 mutation operators implemented by the tool are taken from [6], [13], [16] and presented in Table I. The first four operators respectively remove and negate one literal or one clause within the formula. The last two operators transforms an AND into an OR and vice-versa.

The application of these operators to the example formula give the mutants listed in Table II. Here, it should be noted that the application of the operators can add or remove clauses within the formula, and that none of the resulting mutant is an invalid formula.

B. Evaluation of the Mutation Score

The second step of the approach checks whether for each mutant created there is one test case in the test suite that kills it. To this end, a satisfiability (SAT) solver is used to evaluate the satisfiability of the formula given the variables assignment of the test case. SAT solver are widely used to evaluate constrained boolean expressions, e.g. [17]. As a result, for each mutant, it is evaluated whether there is one test case that does not satisfy the formula. When such a test case exist, the mutant is said to be killed.

Considering the example, the 9 mutants underlined in Table II are killed by the test cases. It means that the two assignments of tc1 and tc2 satisfy the other mutants. Thus, the mutation score achieved by this test suite is \( \frac{9}{20} = 60\% \).

V. THE MUTALOG TOOL

MutaLog is an open source\(^1\) Java application of around 2,000 lines of code\(^2\) in its current version. It implements the mutation analysis approach for logic formulas presented in the previous section.

A. Features

MutaLog allows performing the following actions:
- Loading a logic formula from a file. MutaLog supports the DIMACS (Conjunctive Normal Form) format,
- Visualizing the clauses of the formula,
- Creating mutants of the formula by applying the operators presented in the previous section,
- Loading a test suite and visualize the test cases,
- Evaluating the mutation score of the test suite towards the formula mutants.

\(^{1}\)The code source is available at https://github.com/christopherhenard/mutalog
\(^{2}\)Measured with cloc http://cloc.sourceforge.net/

B. Architecture

1) General: MutaLog is built upon the Model-View-Controller (MVC) architecture [18]. This architecture allows separating the internal representation of the information and its logic (the model) from the graphical representation (the view) and the user’s interaction with it (the controller(s)). Concretely, the model, which corresponds to the business logic of the application is observed by the view, which graphically represents the model. When the user performs an action on the graphical interface, a controller acts on the model to change its internal representation which triggers the view to be refreshed. The main advantage of this architecture is the separation of concerns and the code reusability.

To implement the MVC architecture, the application is organized into packages. It means that the Java classes are grouped into a conceptually coherent way depending on their functionalities. Thus, the core package corresponds to the model while the gui package contains the classes related to the views and controllers. Figure 1 represents the package architecture of the application. The tool also makes use of common design patterns [19], like or the adapter pattern to map the model of complex graphical component to the tool’s model or the observer pattern to implement the MVC architecture.

2) MutaLog’s Main Components: The architecture of MutaLog is presented on Figure 2. MutaLog takes as input the logic formula and the test suite. From the logic formula, the formula mutants are created by the mutant operators. Then, using a satisfiability (SAT) solver, the test suite is evaluated towards the mutants. Finally, the mutation score is returned.

3) The core package: This package contains the classes related to the business logic of the application (the model). The class diagram of this package and its sub-packages is
In the following, we describe the role of each class:

- **core.ModelMutaLog**: This class is the model of the application, it contains the main business logic, like the possibility to load a logic formula,
- **core.CNFFormula**: This class represents a logic formula under the CNF format,
- **core.Clause**: This class represents a clause of the CNF formula,
- **core.Literal**: This class represents a literal of a clause,
- **core.Mutant**: This class represents a mutated logic formula,
- **core.TestSuite**: This class represents a test suite for a logic formula,
- **core.Test**: This class represents a given test case of the test suite.

### C. Libraries

MutaLog uses two external libraries in addition to the standard Java library:

- **Sat4J**[^3], which provides an efficient SAT solver for Java and which is used to generate valid configuration of the FM (product variants),
- **JCommander**[^4], which simplifies the parsing of command line arguments and which is used for the command line interface of the tool.

### D. Usage

The MutaLog tool can be used with both a command line interface (CLI) and graphical user interface (GUI). The command line interface eases the use of the tool in a scripting or automated context while the GUI is more user-friendly. Figure 3 provides a screenshot of the GUI. The main window of the application contains a tool bar which provides a quick access to the main functions of the tool.

[^3]: http://www.sat4j.org/
[^4]: http://jcommander.org/

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In terms of end use, an HTML user guide (see Figure 5) is embedded in the application to help the user using the tool. In terms of development, the source code and the Javadoc documentation are available. As the tool is open source, it can be used as a library as well. Finally, it is planned to build an Eclipse plugin to integrate the use of the tool within the Eclipse environment.

VI. RELATED WORK

Generally, the application of mutation testing and analysis to test specifications or models has been widely used [12]. For instance, Li et al. applied mutation analysis on Finite State Machines [7]. Other models include Petri nets [8] or security policies metamodels [9]. In this paper, we focus on logic formulas.

With respect to mutation, several work are related to the present one. In [15], [20], Kaminski et al. use a logic mutation approach to generate only subsuming higher order logic mutants. This approach works in the context of logic-based testing which aims at designing tests depending on logical expressions. In this paper, mutation operators are applied on a logic formula. The objective is to evaluate the quality of a test suite according to the mutants of the formula. In [3], Andrew et al. use mutation analysis to create mutants. They show that generated mutants can be used to predict the detection effectiveness of real fault. They investigate the relative cost and effectiveness of different testing coverage criteria. Here, we do not focus on whether or not the generated mutants are representative of real defects. Finally, Gargantini and Fraser propose a method that generate tests for the possible faults of boolean expressions [21]. Here, we do not focus on test generation. We alter the boolean formula representing the FM.

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Figure 4. MutaLog’s Core Classes

Figure 5. MutaLog’s Documentation
Regarding mutation analysis tools, several tool exist, such as Judy [22], μJava [23] or Javalanche [24]. However, all the existing tools perform mutation analysis of programs. To the best of the authors knowledge, there is no tool which performs mutation analysis of logic formulas.

VII. CONCLUSION AND FUTURE WORK

In this paper, we introduced an open source and freely distributed research tool, MutaLog, which performs logic mutation. The tool allows loading a logic formula, creating various mutants of the formula and evaluating the mutation score of a given test suite. To the best of the authors knowledge, MutaLog is the first tool available which allows performing mutation analysis of logic formulas.

The version of MutaLog presented in this paper is the first one. In future, MutaLog will be extended with additional features, including:
- Addition of new mutation operators,
- Support of additional formats than CNF for boolean logic,
- Support of additional logics, e.g., first order logic,
- Integration into an Eclipse plugin.

Finally, we invite researchers, students and developers to use our tool and/or to contribute to its development:

http://research.henard.net/SPL/MutaLog/

REFERENCES

This appendix presents the plan for the live demonstration of the tool. The presentation will be divided into four parts and will mainly focus at presenting the usage of the tool via the graphical user interface. The command line interface of the tool will be briefly described at the end to demonstrate the different way to use the tool. It should be noted that additional features may be integrated to MutaLog and exhibited the day of the demo, depending on what will be added to the tool by the day of the presentation (see Section VII).

A. Introduction and General Presentation of the Tool

The first part of the presentation will aim at presenting the challenges and objective of the tool. To this end, the notion of logic formulas and mutation analysis will first be introduced. Then, a general overview of the approach performed by the tool will be described. Finally, the main features as long as the architecture and usage of MutaLog will be presented.

B. Evaluation of the Mutation Score of a Logic Formula

Here, we will describe the use of MutaLog to evaluate the mutation score of a given test suite. To this end, we will first show how to load a logic formula into the tool. Details about the DIMACS format for CNF logic formulas supported by the tool will be given. Then, we will present the part of the graphical user interface displaying the information (e.g., the clauses) regarding the loaded formula.

After presenting how to load a test suite into the application, we will show how to evaluate the mutation score. To this end, the different mutation operators that can be applied on the formula will be described (see Figure 6). Finally, we will present the result of the tool: the mutation score and the list of mutants produced by the operators (see Figure 7). The mutants that are killed are displayed in red and the invalid mutants are stroked. The other mutants that are displayed are mutants not killed by any test case of the test suite.

C. Command Line Interface, Documentation and Future Improvements

The last part of the presentation will first briefly demonstrate the command line interface of the tool. Then, the embedded and online documentation of MutaLog will be presented. Figure 8 illustrates a screenshot of this documentation embedded in the application.

Finally, the forthcoming features to be added to the tool will be presented. The presentation will end with a questions/answers session. The objective of this session is to get a first feedback on the tool.

http://research.henard.net/SPL/MutaLog/doc/